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# Advertising pricing models in media markets: Lump-sum versus per-consumer charges $\overset{\scriptscriptstyle \,\mathrm{thet}}{\sim}$

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#### ABSTRACT

Based on a model of asymmetric competition between a pay and a free media platform, this paper investigates advertising pricing models. The pay media platform generates revenues from media consumers through subscription fees, while the free media platform generates revenues from charging advertisers either on a lump-sum basis (regime A) or on a per-consumer basis (regime B). We show that the free platform produces a higher advertising level and attracts more consumers in regime A than B although advertisers must pay more for ads and consumers dislike ads. Moreover, the pay media platform faces higher subscription fees and lower consumer demand in regime A than B. Compared to regime B, the profit of the free (pay) media platform is higher (lower) in regime A, while aggregate profits are higher only if the consumers' disutility from ads is sufficiently low. In addition, advertisers are better off in regime A than B, while the opposite is true for the media consumers. Finally, in small media markets, social welfare is lower in regime A than B, while this is true in large media markets only if the media consumers' disutility from advertising is sufficiently high.

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#### 1. Introduction

Two generic business models coexist and compete in the various media markets: either media platforms provide their content to the media consumers for free and generate revenues from advertising (free media platform), or media platforms do not place ads but charge their consumers a subscription fee for access to their contents (pay media platform).<sup>1</sup> Free media platforms possess two basic ways to charge advertisers. Advertisers are charged a lump-sum fee for placing ads or they are charged on a per-consumer basis so that the advertising charges are a positive function of the consumer size. For example, an online media platform can ask advertisers a certain fixed amount for placing ads during a certain time period (lump-sum charges) or it can charge advertisers via the concept of Pay-per-Click or







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<sup>&</sup>lt;sup>1</sup> A third hybrid business model exists where media platforms place ads and charge consumers (e.g., daily newspapers and magazines). However, in this paper we focus on the two generic models: pay vs free platforms. One justification for the coexistence between pay and free media platforms is that media consumers usually dislike the presence of ads because they decrease the entertainment value of consuming the media content, see Depken and Wilson (2004), Anderson and Coate (2005), Wilbur (2008), and Casadesus-Masanell and Zhu (2010). As a result, some media consumers are willing to pay for media content and are switching to ad-free pay platforms to avoid ads (Tåg, 2009b).

Cost-per-Click where advertisers must pay for each click on the ad link (per-consumer charges). Other examples for perconsumer advertising charges include pricing models such as CPM (cost per thousand impressions/views), CPA (cost per action, where the required action is defined by the advertisers, e.g., signing up for a service or ordering products etc.), and CPV (cost per view/visitor). Particularly, Google applies the pricing model "AdWords" where advertisers create their ads and choose keywords which are related to their business. When consumers search one of the keywords on Google or use relevant Google services such as Google Mail, the corresponding ads appear next to the search results and advertisers have to pay only if consumers click on the ads rather than paying a lump-sum charge for their ads.

Yet, are per-consumer advertising charges really the optimal pricing strategy for a media platform and is the shift towards consumer-based instead of lump-sum advertising charges socially desirable? Based on a simple theoretical model of a media market that is served by one pay media and one free media platform, this paper tries to answer these and related questions by formally investigating the economic effects of the two distinct advertising pricing models on relevant outcomes such as platform profits, consumer and advertiser surpluses as well as social welfare. We conduct our analysis in a framework of asymmetric competition because such a setting is common in the real world but has been widely neglected in the existing literature. Asymmetric competition between a pay and a free media platform exists across a broad range of industries. For instance, pay TV channels compete against free TV Channels (e.g. HBO vs. CBS), subscription newspapers compete against free newspapers (e.g. Wall Street Journal vs. USA Today), fee-based webmail providers compete against free webmail providers (e.g. Yahoo! Mail Plus vs. Gmail), and paid dating platforms compete against free dating platforms (e.g. eHarmony vs. POF). In accordance with the existing literature (e.g., Anderson and Coate, 2005; Peitz and Valletti, 2008), we model media competition in the Hotelling fashion. That is, the media consumers consume ad-free media content on the pay platform and pay a positive subscription fee or they consume the media content for free and accept the presence of advertising. The free media platform can charge its advertisers either a lump-sum charge (regime A) or on a per-consumer basis (regime B). In regime A, the advertisers pay a fixed amount for placing an ad on the free media platform, which does not explicitly depend on the consumer size. In regime B, the price that advertisers must pay for placing an ad is an increasing function of the consumer size. To analyze these two pricing models, we model the advertising market explicitly and assume that advertiser demand positively depends on the consumer size.

Our model shows that the dominant pricing strategy for the free media platform is to apply lump-sum charges for the advertisers because it realizes higher profit compared to a per-consumer advertising charge. Moreover, the advertising level on the free platform is higher and the platform attracts more consumers under lump-sum charges although advertisers must pay more per ad and consumers dislike ads. We find that the competing pay media platform's profit is lower if the free platform imposes a lump-sum charge on advertisers because the lower consumer demand overcompensates for the higher subscription fee. As a result, the strength of media consumers' disutility from ads determines whether aggregate profits are higher in regime A or B. Moreover, the advertisers are always better off and the media consumers are worse off if the advertiser charge is levied on a lump-sum basis. Overall, in small media markets, applying lump-sum advertiser charges always yields lower social welfare; in large media markets, this finding is true only if the media consumers' disutility from ads is sufficiently high.

In the remainder of the paper we proceed as follows. In the next section, we review the related literature. Section 3 introduces the basic model setup and Section 4 provides the equilibrium analysis. In Section 5, we compare the relevant outcomes of both regimes and derive our main results. Section 6 discusses the robustness of the results. Section 7 concludes the paper.

#### 2. Related literature

Our analysis of asymmetric competition between a pay media platform and a free media platform that charges advertisers contributes to the literature on the economics of media markets in two dimensions.<sup>2</sup> First, we add to this literature by comparing lump-sum and per-consumer advertiser charges in an integrated framework. Second, we contribute to the literature because prior research focuses on symmetric competition between either free media platforms or pay media platforms and then compares the two independent scenarios separately.

In the area of media economics, most papers that explicitly model the advertising market explore one of the two advertising pricing models (lump-sum or per-consumer charges). Papers that assume a lump-sum advertising charge include, e.g., Gabszewicz et al. (2001), Crampes et al. (2009), Kind et al. (2009), and Reisinger (2011).

Gabszewicz et al. (2001) develop a model in which two symmetric competing newspapers play a three-stage game and sequentially set the political opinion, the prices of newspapers, and the advertising prices. They show that newspaper editors often tend to sell tasteless political messages to their readers in order to augment the audience size and therefore to become more attractive to advertisers. Crampes et al. (2009) present a model of media competition with free entry by considering the number of active media platforms as endogenous.<sup>3</sup> In their model of symmetric competition, the media platforms are either financed with advertising and subscription revenues or they are solely funded by advertising receipts. The authors find that under constant or increasing returns to scale in the audience size, there are an excessive number of firms and underprovision of advertising in the markets. Kind et al. (2009) investigate how the number of the media platforms and the level of horizontal differentiation between media platforms could affect the way media firms raise their revenues. They demonstrate that symmetric media platforms generate less

 <sup>&</sup>lt;sup>2</sup> For a summary of the literature, see Anderson and Gabszewicz (2006).
 <sup>3</sup> See also Choi (2006) for a model of broadcast competition with free entry.

revenue from consumers when the horizontal differentiation is low. Media firms also generate less revenue from advertisers when there are more firms in the markets. Reisinger (2011) presents a two-sided market model of symmetric free media platforms that compete for advertisers and consumers. He also extends his model to a setting in which platforms charge consumers for the consumption of the platform's content. He shows that media platforms' profits can increase with users' nuisance cost of ads.

Models with a per-consumer advertising charge can be found, for example, in Anderson and Coate (2005) and Peitz and Valletti (2008). Anderson and Coate (2005) develop a general theory of market provision of broadcasting and analyze the nature of market failure in this industry. They show that symmetric commercial broadcasters provide advertising levels and programming amounts that can be above or below socially optimal levels, depending on how strongly viewers dislike advertising (among other factors). Peitz and Valletti (2008) focus on the endogenous provision of program diversity by symmetric television broadcasters. They analyze how the program diversity and advertising level (among others) may be affected under two different revenue regimes adopted by the TV broadcasters, pay TV with income from both viewers and advertisers and free TV with only advertising receipts. Broadcasters tend to vertically differentiate their channel programs more when they adopt pay TV than free TV. Moreover, the advertising level is higher under the free TV regime when viewers strongly dislike advertising.

The only paper that explicitly compares lump-sum and per-consumer advertising charges is Armstrong (2006). In his framework of a so-called competitive bottleneck, two media platforms (newspapers) generate revenues from two sources, readers and advertisers. There is competition for readers, but not for advertisers. Under the assumption that readers like (dislike) ads, the equilibrium reader price and platform profit is lower (higher) if platforms charge advertisers on a lump-sum rather than per-reader basis. In contrast to Armstrong (2006), who analyzes the symmetric competition between two pay media platforms (with subscription fees and advertising charges), we consider a scenario of asymmetric competition between one pay media platform (only with subscription revenues) and one free media platform (only with advertising revenues).

In sum, neither of the above-mentioned papers on competition in media markets compares the two advertising pricing models in a framework of asymmetric competition between pay and free media platforms. Thus, our paper can offer insights about a scenario, in which pay and free media platforms coexist and compete for the same consumers. To the best of our knowledge, only a few papers model the direct competition between pay media and free media in a integrated framework.

Casadesus-Masanell and Zhu (2010) develop a model of duopoly competition between a high-quality incumbent and a low-quality ad-sponsored entrant. They investigate what the optimal reaction regarding own business model for the incumbent could be when it faces a new ad-sponsored entrant. They consider four different business models for the incumbent: a subscription-based model; an adsponsored model; a mixed model with both subscription

and ads; and a dual model with two products (one based on the ad-sponsored model and the other based on the mixed model). The case in which the incumbent chooses a subscription-based model is similar to the asymmetric competition in our setting. Lin (2011) studies the endogenous provision of program quality by one pay TV broadcaster and one free TV broadcaster competing directly against each other. He shows that depending on the viewers' nuisance cost of ads and on the degree of horizontal differentiation, pay TV does not always offer higher quality programming than free TV. Dietl et al. (2012) also model asymmetric competition between a pay TV broadcaster and a free TV broadcaster to analyze the economic effects of introducing advertising on the pay TV channel. They show that under certain circumstances there is scope for the pay TV broadcaster to place ads on its channel. By doing so, viewers will always benefit from it while aggregate broadcaster profits may increase if the viewer's disutility from ads is sufficiently high. However, neither of the three aforementioned papers explicitly models the advertising market nor compares the two different advertising pricing models (lump-sum versus per-consumer charges).

Our paper is related also to the literature on two-sided markets.4 Media markets are canonical examples of twosided markets in which media platforms serve two distinct groups of agents, media consumers and advertisers. It is essential for the media platforms to take into account the existence of indirect network effects between media consumers and advertisers. There are positive network effects that operate from media consumers to advertisers such that the value of the media platform for the advertisers increases with the number of media consumers.<sup>5</sup> In contrast, the network effects that operate from advertisers to consumers are considered to be mainly negative in media industries.<sup>6</sup> In our model only the free media platform operates a twosided market strategy while the pay media platform operates in a traditional one-sided market. Although the free media platform does not price both market sides, due to the existence of indirect network effects between advertisers and media consumers, such a platform can also be considered two-sided.

#### 3. Model

We consider a media market with three types of agents: consumers (users), platforms, and advertisers. The media market is served by one pay media platform and one free media platform. The pay media platform charges its consumers a subscription fee for access to the media content whereas the free media platform gives free access to its consumers with no further monetary charges. There are no ads on the pay media platform while the consumers

<sup>&</sup>lt;sup>4</sup> Important works on two-sided markets include Caillaud and Jullien (2003), Rochet and Tirole (2003), Rysman (2004), Armstrong (2006), Hagiu (2006), Kaiser and Wright (2006), Belleflamme and Toulemonde (2009), and Weyl (2010).

<sup>&</sup>lt;sup>5</sup> See Gabszewicz et al. (2004) and Kind et al. (2007).

<sup>&</sup>lt;sup>6</sup> An exception is Kaiser and Song (2009) who find that in the German magazine market, readers actually appreciate informative ads, such as car ads in car magazines.

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are exposed to ads on the free media platform. We differentiate two pricing regimes for advertisers: lump-sum and per-consumer charges.

#### 3.1. Consumers

Suppose there are  $\theta \in \mathbb{R}^+$  media consumers uniformly distributed along the unit interval. The two media platforms are located at the extremes of the unit interval where the pay media platform (denoted by subscript *p*) is situated at 0 and the free media platform (denoted by subscript *f*) is situated at 1. We consider the Hotelling model with linear transport cost of  $t \in \mathbb{R}^+$  per unit of length. Hence, the two media platforms are horizontally differentiated from the perspective of consumers and the parameter *t* can be interpreted as the differentiation parameter. A lower value of *t* means that the media platforms (or rather their media content) are perceived as closer substitutes by the consumers.

The indirect utility function of a consumer located at point  $x \in [0, 1]$  when consuming media on the pay media platform or on the free media platform is given by

$$u_p = v - s_p - tx,\tag{1}$$

$$u_f = v - \gamma a_f - t(1 - x), \tag{2}$$

where  $s_p$  is the subscription fee and  $a_f$  is the level of advertising on the free media platform. The parameter  $v \in \mathbb{R}^+$ denotes the consumers' intrinsic value from consuming media (Economides and Tag, 2012) and the parameter  $\gamma \in \mathbb{R}^+$  measures the level of consumers' disutility from ads.<sup>7</sup> We assume full consumer market coverage, i.e., the consumers' intrinsic value from consuming media is sufficiently large such that all consumers will join one media platform. We also assume that no media platform can corner the consumer market such that each media platform gains a positive market share. The marginal consumer, who is indifferent between consuming pay media and free media, is located at  $\bar{x} = \frac{1}{2} + \frac{1}{2t}(\gamma a_f - s_p)$ . All consumers to the left of  $\bar{x}$ consume the content of the pay media platform and all consummers to the right of  $\bar{x}$  consume the content of the free media platform. As a result, the demand function of the pay media and free media consumers, respectively, are given by

$$n_p = \frac{\theta}{2} \left[ 1 + \frac{1}{t} \left( \gamma a_f - s_p \right) \right],\tag{3}$$

$$n_f = \theta - n_p = \frac{\theta}{2} \left[ 1 + \frac{1}{t} (s_p - \gamma a_f) \right].$$
(4)

The consumers of the pay media and free media derive the following surpluses:

$$CS_{p} = \theta \int_{0}^{x} (\nu - s_{p} - tz) dz \quad \text{and}$$
  

$$CS_{f} = \theta \int_{\bar{x}}^{1} (\nu - \gamma a_{f} - t(1 - z)) dz.$$
(5)

Because the consumer market is fully covered, the aggregate consumer surplus is the sum of all consumers' net benefits from consuming media,  $CS = CS_p + CS_f$ .

#### 3.2. Advertisers

Advertisers are producers of goods or services who want to attract potential buyers through ads on the free media platform. As in previous studies (see, e.g., Crampes et al., 2009), we assume that each advertiser can place only one ad on the free media platform such that the number of advertisers also represents the number of ads. We assume that the advertisers incur the  $\cos \eta$  for designing and producing one ad. Advertisers are heterogeneous with respect to  $\eta$  where  $\eta$  is assumed to be uniformly distributed in the unit interval,  $\eta \sim U[0; 1]$ . We assume that the net utility of advertisers is given by

$$u_a = \beta n_f - p_f - \eta,$$

where  $\beta \in \mathbb{R}^+$  measures the marginal gross benefit of an advertiser derived from each media consumer and  $p_f$  is the price an advertiser has to pay per ad. An advertiser decides to place an ad if her net utility is non-negative,  $u_a \ge 0$ . By normalizing the mass of advertisers to unity, we derive the advertiser demand as<sup>8</sup>

$$a_f = \beta n_f - p_f.$$

Advertiser surplus is then given by

$$AS = \int_0^{a_f} (\beta n_f - y - p_f) dy.$$
(6)

Advertiser surplus is the positive difference between the amount that advertisers are willing and able to pay for placing an ad and the amount that they actually pay.

#### 3.3. Media platforms

The media platforms provide the content for the consumers. The pay media platform generates its revenues purely from the media consumers through subscription fees, while the free media platform generates its revenues from advertising receipts. For simplicity, all incurring costs for the media platforms are assumed to be 0. The profit functions of the pay and free media platforms, respectively, are then given by

$$\pi_p = s_p n_p$$
 and  $\pi_f = p_f a_f$ 

We consider two advertising pricing models on the free media platform: In regime A, the advertising charge is levied on a lump-sum basis where  $R_f$  denotes the fixed price that each advertiser has to pay per ad, i.e.,  $p_f = R_f$ . In regime B, advertisers are charged on a per-consumer basis where  $r_f$ denotes the charge that each advertiser has to pay per consumer for placing one ad. Hence, in regime B the price per ad positively depends on the number of attracted media consumers, i.e.,  $p_f = r_f n_f$ . Fig. 1 graphically illustrates our model.

<sup>&</sup>lt;sup>7</sup> As mentioned in Section 2, recent works in media industries assume that consumers do not like ads and derive a disutility from it. We follow this approach because it allows us to focus on the trade-off for consumers between ads-free media with a subscription fee and free media that includes ads.

<sup>&</sup>lt;sup>8</sup> For a similar derivation of advertiser demand, see e.g., Li (2009).

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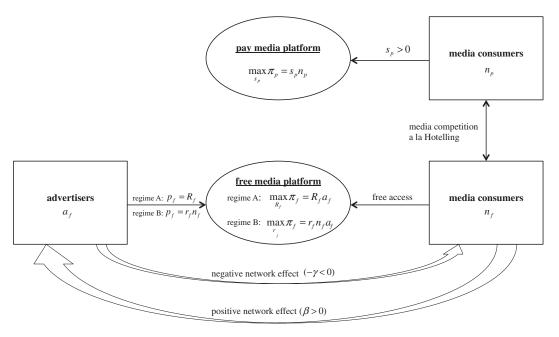


Fig. 1. Model Illustration.

#### 4. Analysis

In this section, we derive the equilibrium outcomes by assuming that both media platforms simultaneously maximize their profits. The pay media platform sets the subscription fee, while the free media platform either sets a fixed price for an ad or sets a per-consumer price for an ad. First, we analyze regime A in which advertisers pay a lump-sum charge. Second, we investigate regime B where advertisers are charged on a per-consumer basis.

#### 4.1. Regime A: lump-sum advertising charges

In regime A, the advertising charge  $R_f$  is levied on a lump-sum basis and hence advertisers derive the net utility  $u_a = \beta n_f - R_f - \eta$ . The advertiser demand function is therefore given by  $a_f = \beta n_f - R_f$ . By substituting this demand function into (3) and (4), we obtain free media and pay media consumer demand in regime A as

$$n_f^A = \frac{\theta}{2t + \theta\beta\gamma}(t + s_p + \gamma R_f) \text{ and } n_p^A = \theta - n_f^A.$$
 (7)

Consequently, the advertising level is given by

$$a_f^A = \beta n_f^A - R_f = \frac{\theta \beta}{2t + \theta \beta \gamma} \left( t + s_p - \frac{2t}{\theta \beta} R_f \right). \tag{8}$$

It is intuitively clear that a higher subscription fee  $s_p$  on the pay media platform decreases consumer demand  $n_p^A$  on this platform and increases consumer demand  $n_f^A$  on the free media platform. As a result, the advertising level  $a_f^A$  on the free media platform also increases with a higher subscription fee. On the other hand, a higher advertising charge  $R_f$  on the free media platform. Because media consumers dislike ads, this reduction in the advertising level leads to a higher free media consumer demand  $n_f^A$  and consequently to a lower pay media consumer demand  $n_p^A$ .

The pay and free media platforms simultaneously solve  $\max_{s_p>0} \left\{ \pi_p^A = s_p n_p^A \right\}$  and  $\max_{R_f>0} \left\{ \pi_f^A = R_f a_f^A \right\}$ , respectively. The equilibrium  $\left( s_p^{A*}, R_f^{A*} \right)$  is then characterized by<sup>9</sup>

$$\frac{\partial \pi_p^A}{\partial s_p} = n_p^A + s_p^A \frac{\partial n_p^A}{\partial s_p} = 0 \text{ and } \frac{\partial \pi_f^A}{\partial R_f} = a_f^A + R_f^A \frac{\partial a_f^A}{\partial R_f} = 0.$$
(9)

The two first-order conditions have an intuitive interpretation. For the pay media platform, a marginally higher subscription fee  $s_p$  induces a direct positive revenue effect  $n_p^A$ and an indirect negative consumer-mediated effect  $s_p^A \partial n_p^A / \partial s_p$  through a reduction in consumer demand. The optimal subscription fee  $s_p^{A*}$  is chosen such that the revenue effect and consumer effect are balanced.

For the free media platform, marginally increasing the lump-sum advertising charge  $R_f$  triggers a direct positive revenue effect  $a_f^A = \beta n_f^A - R_f$  and an indirect negative advertiser-mediated effect  $R_f^A \frac{\partial a_f^A}{\partial R_f} = R_f^A \left(\beta \frac{\partial n_f^A}{\partial R_f} - 1\right)$  through a lower advertising level. The advertiser effect  $\frac{\partial a_f^A}{\partial R_f}$  is composed of two effects: the first term,  $\beta \frac{\partial n_f^A}{\partial R_f}$ , represents the positive effect on the advertisers through higher consumer demand and the second term, -1, is the negative effect of a higher advertising price. The second effect dominates the first such that  $\frac{\partial a_f^A}{\partial R_f} < 0$ . Again, the platform chooses the optimal advertising price in a way that balances both countervailing effects (i.e., revenue effect and advertiser-mediated effect).

To make the notation simpler, we henceforth write  $\lambda \equiv \theta \beta \gamma$ . By solving the above system of first-order conditions, we compute the subscription fee and the lumpsum advertiser charge in equilibrium as

<sup>&</sup>lt;sup>9</sup> The second-order conditions are satisfied because  $\frac{\partial^2 \pi_p}{\partial s_p^2} = -\frac{2\theta}{2t+\theta\beta\gamma} < 0$  and  $\frac{\partial^2 \pi_f}{\partial t_l^2} = -\frac{4t}{2t+\theta\beta\gamma} < 0$ .

$$\left(s_{p}^{A*}, R_{f}^{A*}
ight) = \left(rac{t(4t+3\lambda)}{8t+\lambda}, rac{ hetaeta(3t+\lambda)}{8t+\lambda}
ight).$$

Hence, each advertiser has to pay  $p_f^{A*} = R_f^{A*}$  per ad on the free media platform. Substituting  $s_p^{A*}$  and  $p_f^{A*}$  into the demand functions yields equilibrium demands of the pay media consumers and free media consumers  $(n_p^{A*}, n_f^{A*})$  as well as the advertising level  $a_f^{A*}$  on the free media platform. Similarly, we obtain equilibrium platform profits  $(\pi_p^{A*}, \pi_f^{A*})$ , aggregate consumer surplus  $CS^{A*}$ , and advertiser surplus  $AS^{A*}$ . See the appendix for a detailed derivation of these outcomes.

#### 4.2. Regime B: per-consumer advertising charges

In regime B, the advertising charge  $r_f$  is levied on a perconsumer basis and the price per ad is  $p_f = r_f n_f$ . Advertisers therefore enjoy a net utility of  $u_a = \beta n_f - r_f n_f - \eta$  and their demand function is given by  $a_f = \beta n_f - r_f n_f$ . With a similar approach as in regime A, we obtain free media and pay media consumer demand in regime B as

$$n_f^B = \frac{\theta}{2t + \theta(\beta - r_f)\gamma} (t + s_p) \text{ and } n_p^B = \theta - n_f^B.$$
(10)

Advertiser demand is then given by

$$a_f^B = n_f^B(\beta - r_f) = \frac{\theta}{2t + \theta(\beta - r_f)\gamma}(\beta - r_f)(t + s_p).$$
(11)

The same qualitative comparative statics for the demand functions hold as in regime A.

The pay and free media platforms solve  $\max_{s_p>0}\left\{\pi_p^B = s_p n_p^B\right\}$  and  $\max_{r_f>0}\left\{\pi_f^B = r_f n_f^B a_f^B\right\}$ , respectively. The equilibrium  $\left(s_p^{B*}, r_f^{B*}\right)$  is then characterized by<sup>10</sup>

$$\frac{\partial \pi_p^B}{\partial s_p} = n_p^B + s_p^B \frac{\partial n_p^B}{\partial s_p} = 0, \qquad (12)$$

$$\frac{\partial \pi_f^B}{\partial r_f} = n_f^B a_f^B + r_f^B \left( \frac{\partial n_f^B}{\partial r_f} a_f^B + n_f^B \frac{\partial a_f^B}{\partial r_f} \right) = 0.$$
(13)

A marginal higher subscription fee induces a direct positive revenue effect  $n_p^B$  and an indirect negative consumer-mediated effect  $s_p \frac{\partial n_p^B}{\partial s_p}$ . For the free media platform, marginally increasing the advertising charge triggers a direct positive revenue effect  $n_f^B a_f^B$  and an indirect effect through changes in  $n_f^B a_f^B$ . This indirect effect is composed of two effects: first, marginally increasing  $r_f$  causes a positive consumer effect  $\frac{\partial n_f^B}{\partial r_f} a_f^B > 0$  through a higher consumer demand level. Second, marginally increasing  $r_f$  induces a negative advertiser effect  $n_f^B \frac{\partial a_f^B}{\partial r_f} < 0$  through a lower advertiser demand level. Which of the two effects dominates depends on the level of  $\gamma$ . We derive  $\frac{\partial n_f^B a_f^B}{\partial r_f} < 0 \iff \gamma < \hat{\gamma} = \frac{2t}{(\beta - r_f)\theta^*}$ . Hence, if the media consumers' disutility from ads is sufficiently low, the positive consumer effect will be dominated by the negative advertiser effect because consumer demand increases to such an extent that it cannot overcompensate for the lower advertising level.

By solving the above system of first-order conditions, we compute the subscription fee and the per-consumer advertising charge in equilibrium as

$$\left(s_{p}^{B*},r_{f}^{B*}
ight)=\left(rac{t(4t+3\lambda)}{2(4t+\lambda)},rac{eta(2t+\lambda)}{4t+\lambda}
ight)$$

Substituting  $s_p^{B*}$  and  $r_f^{B*}$  into the demand functions yields equilibrium demands of the pay and free media consumers  $\binom{n_p^{B*}, n_f^{B*}}{n}$  as well as the advertising level  $a_f^{B*}$  on the free media platform. We further derive that each advertiser has to pay

$$p_f^{B*} = r_f^{B*} n_f^{B*} = \frac{\beta \theta (12t + 5\lambda)}{8(4t + \lambda)}$$

per ad. Analogous to above, we obtain equilibrium platform profits  $(\pi_p^{B_*}, \pi_f^{B_*})$ , aggregate consumer surplus  $CS^{B_*}$ , and advertiser surplus  $AS^{B_*}$ . See the appendix for a detailed derivation of these outcomes.

#### 5. Comparison of equilibrium outcomes

In this section, we compare the outcomes of the two regimes. First, we compare the subscription fees on the pay media platform and the prices advertisers must pay for an ad placed on the free media platform.

#### **Proposition 1.**

- (i) The subscription fee that a consumer must pay on the pay media platform is higher in regime A than in regime B, i.e., s<sub>p</sub><sup>A\*</sup> > s<sub>p</sub><sup>B\*</sup>.
- (ii) The price that an advertiser must pay per ad on the free media platform is higher in regime A than in regime B, i.e., p<sub>f</sub><sup>A\*</sup> > p<sub>f</sub><sup>B\*</sup>.

#### **Proof.** See Appendix B.1.

Part (i) posits that the pay media platform charges consumers a higher subscription fee if the free media platform chooses a lump-sum advertiser charge as compared to a per-consumer charge. To understand the intuition behind this result, we rearrange the first-order conditions (9) and (12) to obtain

$$\frac{\theta}{2t+\lambda} \left( t + \lambda - \gamma R_f^A - s_p^A \right) = s_p^A \left( \frac{\theta}{2t+\lambda} \right), \tag{14}$$

$$\frac{\theta}{2t + \theta \gamma \left(\beta - r_f^B\right)} \left(t + \lambda - \gamma \theta r_f^B - s_p^B\right) = s_p^B \left(\frac{\theta}{2t + \theta \gamma \left(\beta - r_f^B\right)}\right).$$
(15)

The left-hand side (lhs) of both equations represent the revenue effect  $n_p$ , while the right-hand sides (rhs) characterize the consumer-mediated effects  $s_p\left(-\frac{\partial n_p}{\partial s_p}\right)$ . Substituting the best-response functions  $R_f^A(s_p^A) = \frac{\theta\beta(t+s_p^A)}{4t+\theta\beta\gamma}$  and  $r_f^B = \frac{\beta(2t+\theta\beta\gamma)}{4t+\theta\beta\gamma}$  into (14) and (15), we obtain the following results. For a given subscription fee  $s_p$ , the revenue effects (lhs) are equal in both regimes, while the consumer-med-

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<sup>&</sup>lt;sup>10</sup> The second-order conditions are satisfied because  $\frac{\partial^2 \pi_p}{\partial s_p^2} = \theta\left(-\frac{1}{2t} - \frac{1}{2t+\lambda}\right) < 0$  and  $\frac{\partial^2 \pi_f}{\partial r_f^2} = -\frac{\theta^2 (4t+\lambda)^2 (12t+5\lambda)^2}{256t(2t+\lambda)^3} < 0.$ 

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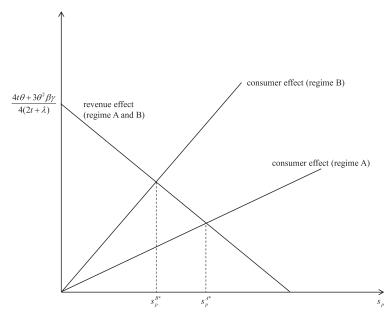


Fig. 2. Intuition for Proposition 1.

iated effects (rhs) are stronger in regime B than in regime A. Hence, increasing the subscription fee decreases the revenue effects with equal strength in both regimes, while the consumer effect increases more strongly in regime B than in A. As a result, the equilibrium subscription fee is larger in regime A than in B, i.e.,  $s_p^{A*} > s_p^{B*}$ . Fig. 2 depicts these effects as a function of the subscription fee  $s_p$ .

According to part (ii), the per-ad price  $p_f^{A*} = R_f^{A*}$  that each advertiser must pay if it is charged on a lump-sum basis is higher than the per-ad price  $p_f^{B*} = r_f^{B*} n_f^{B*}$  if it is charged on a per-consumer basis. The intuition behind this result is as follows. In both regimes, marginally increasing the advertising charge induces a positive revenue effect and a negative advertiser effect. However, an additional effect is present in regime B: the platform takes into account that a higher advertising charge induces a higher consumer demand (positive consumer effect), which enters the firstorder condition with a positive sign. This effect is not present in regime A because advertisers are charged on a lumpsum basis. As a result, we derive

$$p_f^A(s_p^A) = rac{ hetaetaeta(t+s_p^A)}{4t}$$
 and  $p_f^B(s_p^B) = rac{ hetaeta(t+s_p^B)}{4t}$ 

Because we know that the subscription fee is higher in regime A than in B, i.e.,  $s_p^{A*} > s_p^{B*}$ , it must be the case that  $p_f^{A*} > p_f^{B*}$ .

In the next proposition, we compare both regimes with respect to consumer demands and advertising level.

#### **Proposition 2.**

- (i) The free (pay) media platform attracts more (fewer) consumers in regime A than in regime B, i.e., n<sub>f</sub><sup>A\*</sup> > n<sub>f</sub><sup>B\*</sup> and n<sub>p</sub><sup>A\*</sup> < n<sub>p</sub><sup>B\*</sup>.
- (ii) The advertising level on the free media platform is higher in regime A than in regime B, i.e.,  $a_f^{A*} > a_f^{B*}$ .

**Proof.** See Appendix B.2.  $\Box$ 

Even though the advertising level on the free platform is higher in regime A than in B, part (i) of the proposition posits that this platform attracts more consumers in regime A than in B. To understand the intuition behind this result, recall that the subscription fee on the pay media platform is higher in regime A than in B and consumer demand on the free media platform is given by  $n_f = \frac{\theta}{2} \left[ 1 + \frac{1}{t} (s_p - \gamma a_f) \right]$ . Increasing the subscription fee on the pay platform decreases consumer demand on this platform, and in turn, increases consumer demand on the free platform. Hence, the higher subscription fee on the pay platform in regime A compared to B, overcompensates for the higher advertising level on the free platform such that the free media consumer demand is higher in regime A than in B. Due to our Hotelling specification, it follows that the pay media consumer demand is higher in regime B than in A.

Part (ii) of the proposition shows that the free platform attracts more advertisers in regime A than in B. This result is true despite a higher price per ad in regime A than in B. However, the free platform attracts more consumers in regime A than in B, which makes it more attractive for advertisers to place ads. We conclude that the higher consumer demand overcompensates for the higher price in regime A compared to B.

Next, we compare the profits of the media platforms in both regimes and establish the following proposition:

#### **Proposition 3.**

- (i) The profits of the free (pay) media platform is higher (lower) in regime A than in regime B, i.e., π<sup>A\*</sup><sub>f</sub> > π<sup>B\*</sup><sub>f</sub> and π<sup>A\*</sup><sub>p</sub> < π<sup>B\*</sup><sub>p</sub>.
- (ii) Aggregate platform profits are higher in regime A than in regime B if and only if the consumers' disutility from ads is sufficiently low, i.e.,  $\Pi^{A*} > \Pi^{B*} \Leftrightarrow \gamma < \gamma^{\pi}$ .

#### **Proof.** See Appendix B.3. $\Box$

Part (i) of the proposition states that the free media platform generates higher profits if it prices advertisers via a lump-sum charge as compared to a per-consumer charge. Recall that profits of the free platform are given by  $\pi_f = p_f a_f$ . Because each advertiser must pay a higher price  $p_f$  per ad in regime A than in B, and in addition, the advertising level  $a_f$  is also higher in regime A than in B, the claim follows immediately. Regarding the pay media platform, we find that this platform generates higher profits  $\pi_p = s_p n_p$  if the free platform charges advertisers on a per-consumer basis as opposed to a lump-sum charge. Recall that the subscription fee is lower but consumer demand on the pay platform is higher in regime B compared to A. Hence, the higher consumer demand overcompensates for the lower subscription fee such that profits of the pay platforms are higher in regime B than in A.

Part (ii) shows that whether aggregate platform profits is higher in regime A or B crucially depends on the consumer preferences towards ads. If the consumers sufficiently dislike ads then aggregate profits are higher in the case that the free platform charges advertisers on a per-consumers basis. If, however, the consumers' disutility from ads is sufficiently low then aggregate profits are higher in the case that the free platform charges advertisers on a lump-sum basis.

To understand the intuition behind this result, we analyze how the components of the profit functions react to changes in the disutility parameter of ads  $\gamma$ . For the pay media platform, the subscription fee increases with  $\gamma$  in both regimes and the increase is stronger in regime A than in B. Hence, the spread between the subscription fees augments in  $\gamma$ . The effect of  $\gamma$  on consumer demand  $n_p^{A*}$  in regime A is ambiguous, while the effect is positive on consumer demand  $n_p^{B*}$  in regime B. Overall, the spread between  $n_p^{B*}$  and  $n_p^{A*}$  increases in  $\gamma$ . It follows that the difference in pay media profits  $\Delta_p = \pi_p^{B*} - \pi_p^{A*}$  between regime B and A also augments in  $\gamma$ . Regarding the free media platform, it is intuitive that the advertising level  $a_t^*$  on the free media platform in both regimes decreases in  $\gamma$ . However, it depends on the level of  $\gamma$  whether the decrease is stronger in regime A or B. Furthermore, the price  $p_f^*$  that advertisers have to pay for placing an ad increases in  $\gamma$  because a higher level of  $\gamma$  leads to a lower advertising level which, ceteris paribus, increases advertisers' willingness to pay. The increase in the price for the advertisers is more pronounced in regime A than B such that the price spread between regime A and B augments for an increasing  $\gamma$ . Finally, we find that profits  $\pi_f^*$ of the free media platform decreases with  $\gamma$  in both regimes but it depends on the level of  $\gamma$  in which regime the decrease in profits is more pronounced. Particularly, the difference in free media profits  $\Delta_f = \pi_f^{A*} - \pi_f^{B*}$  between regime A and B reaches its maximum for low values of  $\gamma$  and then diminishes for higher values of  $\gamma$ .

Overall, we conclude that for low values of  $\gamma$  the difference in free media profits  $\Delta_f$  compensates for the difference in pay media profits  $\Delta_p$  such that aggregate profits are higher in regime A than in B. Because  $\Delta_f$  diminishes and  $\Delta_p$  augments for higher values of  $\gamma$ , a critical value of

 $\gamma = \gamma^{\pi}$  exist above which aggregate profits are higher in regime B than in A.

The next proposition compares aggregate consumer surplus and advertiser surplus in both regimes.

#### **Proposition 4.**

- (i) Aggregate consumer surplus is higher in regime B than in regime A, i.e., CS<sup>B\*</sup> > CS<sup>A\*</sup>.
- (ii) The advertiser surplus is higher in regime A than in regime B, i.e.,  $AS^{A*} > AS^{B*}$ .

#### **Proof.** See Appendix B.4. $\Box$

Part (i) states that the media consumers are better off in regime B than in regime A. This result is intuitive because the consumers benefit from a lower subscription fee and a lower advertising level. In contrast, advertisers enjoy a higher surplus in regime A than in regime B, as stated in part (ii) of the proposition. On one hand, advertisers benefit from higher consumer demand in A compared to B, but on the other hand, they face higher prices. As we know from Proposition 2, the higher consumer demand outweighs the higher price such that the advertising level in A is higher than in B. Overall, the higher advertising level together with the higher consumer demand compensate for the higher price such that the advertiser surplus is higher in A compared to B.

In a final step, we compare social welfare in both regimes. We define social welfare *W*, as the sum of aggregate platform profits, aggregate consumers surplus and advertiser surplus

 $W = \Pi + CS + AS.$ 

We establish the following proposition:

**Proposition 5.** In large media markets (i.e.,  $\theta > \theta'$ ), social welfare is higher in regime B than in regime A if and only if the consumers' disutility from ads is sufficiently high, i.e.,  $W^{B*} > W^{A*} \Leftrightarrow \gamma > \gamma^{W}$ . However, in small media markets (i.e.,  $\theta \leq \theta'$ ), social welfare is always higher in regime B than in regime A regardless of the consumers' disutility from ads.

#### **Proof.** See Appendix B.5. $\Box$

The proposition shows that the welfare effect of charging advertisers on a lump-sum basis or a per-consumer basis depends on the market size of consumers and the consumers' disutility from ads. In large media markets (i.e.,  $\theta > \theta' = \frac{8t}{9\beta^2}$ ) the disutility must be sufficiently low to ensure that social welfare is higher in regime A than in B. If, however, consumers sufficiently dislike ads then the opposite is true. In small media markets, in contrast, social welfare is always higher if advertisers are charged on a per-consumer basis than if they are charged on a lumpsum basis. Fig. 3 illustrates the result for large media markets by depicting social welfare in regime A and B as a function of the disutility  $\gamma$ . For the figure, we set the parameters as follows: N = 50, t = 30, v = 50 and  $\beta = 3.5$ .

The figure shows that in both regimes social welfare is a concave function in  $\gamma$  and that for  $\gamma = 0$ , social welfare would be equal in both regimes. For low values of  $\gamma$ , social

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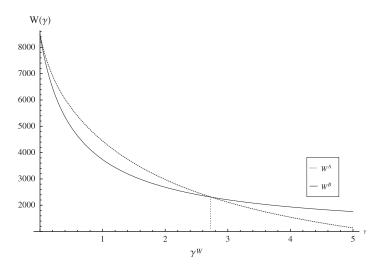


Fig. 3. Social Welfare.

welfare is higher in regime A than in B because welfare decreases with  $\gamma$  stronger in regime B than in A. However, for intermediate values of  $\gamma$ , social welfare decreases less strong in regime B than in A such that there exists a critical value  $\gamma = \gamma^{W}$  for which welfare is equal in both regimes. Above this critical value  $\gamma^{W}$ , welfare is higher in regime B than in A. To understand the intuition behind this result, recall that the aggregate consumer surplus is always lower in A than in B, while the opposite is true for the advertiser surplus. In addition, aggregate platform profits are higher in regime B than in A if the consumers' disutility from ads is sufficiently high. Hence, if  $\gamma$  is low, then the higher advertiser surplus together with the higher aggregate platform profits outweigh the higher aggregate consumer surplus in regime A compared to B such that  $W^{A*} > W^{B*}$ , which is is true as long as  $\gamma < \gamma^{W}$ . If  $\gamma$  increases above this critical value  $\gamma^{W}$ , the difference in the aggregate consumer surpluses between regime B and A is so large that it compensates for the lower advertiser surplus and eventually lower platform profits, yielding a higher level of social welfare in regime B compared to A. In the case of small media markets, this overcompensation of aggregate consumer surpluses between regime B and A is true regardless of the consumers' disutility from ads such that social welfare is always higher in regime B compared to A.<sup>11</sup>

#### 6. Discussion and robustness

In this section, we examine the sensitivity of our results to alternative model specifications, discuss restrictive assumptions of our model and point out possible model extensions.

#### 6.1. Symmetric competition

We examine the sensitivity of our key findings with respect to the nature of competition (symmetric vs. asymmetric competition). In Appendix C, we provide the symmetric baseline case of our model for two free media platforms.<sup>12</sup> We find that the qualitative pattern of results with respect to platform profits, consumer and advertiser surpluses as well as social welfare is consistent between symmetric and asymmetric competition of media platforms. The only exception is aggregate industry profit. Here, we find that for symmetric competition the overall platform profits are unambiguously higher in regime A than B as compared to the ambiguous result under asymmetric competition (derived in Part (ii) of Proposition 3).

We conclude that independent of whether the media industry is served by free media platforms (symmetric competition) or by mixed media platforms (asymmetric competition), the welfare implications of the two different advertising pricing models (lump-sum and per-consumer charges) remain qualitatively the same. Of course, the absolute levels of the equilibrium outcomes differ across the scenarios.

As mentioned in Section 2, the existing literature focuses on symmetric competition between free media platforms in order to investigate the economic effects of lump-sum and per-consumer charges. For example, Armstrong (2006) shows that two symmetric media platforms, which generate revenues from both advertisers and ad-averse consumers, realize higher profit when they charge advertisers on a lump-sum rather than on a perconsumer basis. We obtain the same results regarding platforms profit as Armstrong (2006) if we consider symmetric competition between two free media platforms. Yet, Armstrong (2006) does not analyze the welfare implications of the two advertising pricing models. Our paper, in contrast, sheds light on the effects of the two pricing models on consumer and advertiser surpluses as well as social welfare for both symmetric and asymmetric competion.

<sup>&</sup>lt;sup>11</sup> Formally, the differences of aggregate platform profits as well as advertiser surpluses between regimes B and A decrease more strongly than the respective difference of consumer surplus between regimes A and B for low parameters of  $\theta$ .

<sup>&</sup>lt;sup>12</sup> We do not provide the symmetric baseline case for pay media platforms because (i) it represents the standard Hotelling model in traditional one-sided markets and (ii) the focus of our paper is on distinct advertising pricing models for free media platforms.

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# 6.2. Heterogeneous consumers with respect to the disutility from ads

In our paper, we followed the standard literature in media economics (e.g., Anderson and Coate, 2005; Armstrong, 2006; Peitz and Valletti, 2008) and adopted the Hotelling approach by assuming that the two media platforms are horizontally differentiated from the perspective of consumers. The parameter t represents the differentiation parameter, where a lower value of t characterizes platforms whose media content is perceived as closer substitutes by the consumers. Given our model of asymmetric competition between pay media without ads and free media with ads, an alternative modeling approach would be to consider media consumers that are heterogeneous with respect to their disutility derived from ads. That is, not all consumers dislike ads to the same extent as it is assumed in our model.<sup>13</sup> The introduction of heterogeneous consumers with respect to the disutility from ads would yield media platforms that are perceived as vertically rather than horizontally differentiated. Hence, the pay media platform caters to the ad-averse consumers while the free media platform is more attractive to the less ad-averse consumers. As a result, the profit of the pay media platform is expected to increase in the consumers' disutility from ads, while the opposite is true for the free media platform. Depending on whether the profit effect is more pronounced in regime A or B, it could reverse our results regarding aggregate platform profits derived in Proposition 3. Similarly, our results regarding social welfare crucially depend on whether the advertiser and consumer effect is more pronounced in regime A or B.

However, given that the two media platforms provide different content, our assumption of horizontal rather than vertical differentiation seems to be plausible because we believe that the consumers' choice for adopting one media platform more likely depends on their taste for media content rather than their (dis) taste for ads.

#### 6.3. Quality provision of media content

In addition to ad-free content, pay media platforms often provide high-quality content such as Hollywood Blockbusters or exclusive premium sports channels. As we have recently seen a shift towards more free adbased media, one might ask whether program quality decreases if free ad-based media platforms start competing with pay media platforms. Lin (2011) already addressed this issue and investigated endogenous quality provision by television channels in three scenarios: (i) symmetric competition between two pay TV channels, (ii) symmetric competition between two free TV channels, and (iii) asymmetric competition between one pay TV and one free TV channel. The model shows that the incentives to offer programming quality depend mainly on the nuisance cost of adverting for viewers, the broadcaster's marginal return on advertising, and the degree of horizontal differentiation between the competing channel programs. Particularly, asymmetric competition between a free media and pay media platform affects the overall level and the allocation of program quality between television broadcasters. Whether pay TV or free TV offers higher program quality depends on the extent to which the channel programs are perceived as substitutes and on the nature of competition (symmetric vs asymmetric competition). Under symmetric competition, the program quality on pay TV is always higher than on free TV, while this result does not always hold under asymmetric competition. Here, depending on the degree of horizontal differentiation between the channel programs, it can be the case that the program quality on pay TV is lower than on free TV.

By integrating endogenous provision of content quality by media platforms into our model of asymmetric competition would significantly increase the complexity of the model because both media platforms would then have an additional strategic variable at their disposal. Because in this case, the model would be no longer analytically tractable, we abstract from such an extension and leave it for further research in a setting which is tailored towards this question.

# 6.4. Two-part tariff, market coverage, and endogenous choice of business model

In our paper, we analyzed two basic uniform advertising charges (lump-sum and per-consumer charge) but we neglected the aspect of a two-part tariff to advertisers. Although it would be interesting to examine whether our results still hold under any convex combination of the two uniform pricing regimes, extending the current model to a two-part tariff has proven to be less than straightforward. We faced the issue of multiple equilibria implying a continuum of possible best solutions.

Moreover, within the Hotelling specification we have assumed that the media market is fully covered. It would be interesting to allow for demand expansion effect ("hinterlands" in the Hotelling model) and see whether and how our results change. Such an extension must take into account that demand expansion effects could interact with the inter-side externalities between consumers and advertisers on the free media platform in a non-trivial way.<sup>14</sup> An alternative way to consider an uncovered media market is to specify media consumers' preferences with a quadratic utility function as shown in Kind et al. (2007) and Kind et al. (2009).

Finally, we assumed asymmetric competition in which a pay media platform competes with a free media platform. A more general game should allow media platforms to choose their business model endogenously. It would be interesting to examine whether the asymmetric competitive situation that we study can be an equilibrium outcome of the more general game. For example, Tåg (2009a) shows in a two-sided market model in which competing platforms (technology firms) may prefer to be one-sided

<sup>&</sup>lt;sup>13</sup> We are grateful to an anonymous referee who suggested providing a discussion of our assumption regarding horizontal differentiation.

<sup>&</sup>lt;sup>14</sup> We are grateful to an anonymous referee who pointed this out.

and restrict third party application development (in our setting advertisers) because it removes network effects and thereby relaxes competition for consumers. Interestingly, in his setting with positive externalities between the groups, an asymmetric market structure can arise as an equilibrium outcome.

#### 7. Conclusion

This paper is motivated by the observation that in reality pay and free media platforms often coexist and directly compete with each other. The existing literature, however, widely neglects to model asymmetric competition in media markets. To begin filling this research gap, we develop a simple model of asymmetric competition between a pay media platform and a free media platform. Specifically, we examine how different advertising pricing models (lump-sum versus per-consumer charges) affect relevant equilibrium outcomes.

Our paper shows that profit-maximizing free media platforms should charge their advertisers on a lump-sum basis rather than a per-consumer basis because in doing so they can realize higher profits. However, from the perspective of a social planner this is not always desirable because, at the same time, the profit of the pay media platform will be lower such that the effect on aggregate platform profits depends on the media consumers' disutility from ads. Particularly, if the disutility is sufficiently low, aggregate platform profits are higher under lump-sum charges. Furthermore, the advertisers are always better off if they are charged on a lump-sum basis, while the media consumers are better off if advertisers are charged on a per-consumer basis. Hence, choosing one of the two advertising pricing models benefits either the consumers or the advertisers. Finally, our model shows that social welfare is higher if the advertisers are charged on a perconsumer basis when the media market is small, while this is true in large media markets only if the media consumers' disutility from ads is sufficiently high.

Our analysis has implications for policy makers and regulators in the media industries. One common form of advertising regulation is to directly limit the number or length of ads on media platforms through so-called "advertising caps." Our results suggest another indirect instrument could achieve the aim of low advertising levels. According to our model, the prohibition of lump-sum advertising charges and the enforcement of per-consumer charges lead to a lower advertising level on free media platforms. Such an enforced per-consumer advertising charge could be particularly relevant for the television broadcasting industry where lump-sum advertising charges are predominant due to the difficulty of measuring the exact number of free TV viewers. However, policy makers and regulators should be aware of the resulting welfare effects of such a regulation because in large media markets social welfare could decrease through per-consumer charges, especially if the consumers' disutility from ads is low.

Regarding the question raised in the introduction whether per-consumer advertising charges are socially desirable, we conclude that the answer depends on two critical factors: the size of the media market and the level of consumers' disutility from ads. In media markets with a relatively small audience size, it is desirable from the perspective of a social planner that free media platforms adopt per-consumer advertising charges. This insight can also be applied to large media markets with highly ad-averse consumers. However, if the consumers in large media markets are less ad-averse, policy makers should create better incentives for charging lump-sum advertising fees or take regulatory measures to hinder per-consumer charges. More important, policy makers should be technically able to assess the values of both relevant parameters (i.e., media market size and consumers' disutility from ads) correctly and reliably before they undertake further actions.

The issues surrounding the implications of different advertising pricing models remain a fertile and important line of inquiry for scholars in media economics.

#### **Appendix A. Equilibrium outcomes**

#### A.1. Regime A

Plugging  $(s_p^{A*}, R_f^{A*})$  into the demand function yields equilibrium demands of the pay media consumers as

$$n_p^{A*} = \frac{\theta t (4t + 3\lambda)}{(2t + \lambda)(8t + \lambda)}$$

On the free media platform, consumer and advertiser demands, respectively, are

$$\left(n_{f}^{A*}, a_{f}^{A*}\right) = \left(\frac{\theta(3t+\lambda)(4t+\lambda)}{(2t+\lambda)(8t+\lambda)}, \frac{2\theta t\beta(3t+\lambda)}{(2t+\lambda)(8t+\lambda)}\right)$$

By noting that the marginal consumer in equilibrium is given by  $\bar{x} = \frac{t(4t+3\lambda)}{(2t+\lambda)(8t+\lambda)}$ , consumer surplus is given by

$$CS^{A*} = \left(\nu - \frac{5t}{2} + \frac{19t^3 + 8\lambda t^2}{27(2t+\lambda)^2} + \frac{10(326t^3 + 37\lambda t^2)}{27(8t+\lambda)^2}\right)\theta > 0,$$

and advertiser surplus is

$$AS^{A*} = rac{2 heta^2 t^2 eta^2 (3t+\lambda)^2}{\left(2t+\lambda
ight)^2 (8t+\lambda)^2}.$$

Equilibrium profits are then given by

$$\begin{split} \pi_p^{A*} &= s_p^{A*} n_p^{A*} = \frac{\theta t^2 (4t + 3\lambda)^2}{(2t + \lambda)(8t + \lambda)^2} \quad \text{and} \\ \pi_f^{A*} &= p_f^{A*} a_f^{A*} = \frac{2t \theta^2 \beta^2 (3t + \lambda)^2}{(2t + \lambda)(8t + \lambda)^2}. \end{split}$$

#### A.2. Regime B

Plugging  $\left(s_p^{B*}, r_f^{B*}\right)$  into the demand function yields equilibrium demands of the pay media consumers as

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$$n_p^{B*} = \frac{\theta(4t+3\lambda)}{8(2t+\lambda)}.$$

On the free media platform, consumer and advertiser demands, respectively, are

$$\left(n_{f}^{B*}, a_{f}^{B*}\right) = \left(\frac{\theta(12t+5\lambda)}{8(2t+\lambda)}, \frac{\theta t\beta(12t+5\lambda)}{4(2t+\lambda)(4t+\lambda)}\right)$$

By noting that the marginal consumer in equilibrium is given by  $\bar{x} = \frac{4t+3\lambda}{8(2t+\lambda)}$ , consumer surplus and advertiser surplus are respectively given by

$$CS^{B*} = \left(\nu - \frac{103t}{64} + \frac{11t^3 + 5\lambda t^2}{16(2t+\lambda)^2} + \frac{4t^2}{4t+\lambda}\right)\theta > 0,$$
  
$$AS^{B*} = \frac{\theta^2 t^2 \beta^2 (12t+5\lambda)^2}{32(2t+\lambda)^2 (4t+\lambda)^2}.$$

Equilibrium profits can be derived as

$$\begin{aligned} \pi_p^{B*} &= s_p^{B*} n_p^{B*} = \frac{\theta t (4t + 3\lambda)^2}{16(2t + \lambda)(4t + \lambda)} \quad \text{and} \\ \pi_f^{B*} &= p_f^{B*} a_f^{B*} = \frac{t \theta^2 \beta^2 (12t + 5\lambda)^2}{32(2t + \lambda)(4t + \lambda)^2}. \end{aligned}$$

#### **Appendix B. Proofs**

#### B.1. Proof of Proposition 1

**Part (i).** This part posits that the subscription fee is higher in regime A than in regime B  $(s_p^{A*} > s_p^{B*})$ . This proof is straightforward and thus omitted.

**Part (ii).** This part claims that the advertiser's price per ad is higher in regime A than in regime B, i.e.,  $p_f^{A*} > p_f^{B*} = r_f^{B*} n_f^{B*}$ . We derive

$$\begin{split} p_f^{A*} &> p_f^{B*} \Longleftrightarrow \frac{\theta \beta (3t+\lambda)}{8t+\lambda} > \frac{\beta (2t+\lambda)}{4t+\lambda} \frac{\theta (12t+5\lambda)}{8(2t+\lambda)} \\ &= \frac{\theta \beta (12t+5\lambda)}{32t+8\lambda}. \end{split}$$

We rearrange the inequality in the following way and obtain

$$\theta\beta(3t+\lambda)(32t+8\lambda)-\theta\beta(12t+5\lambda)(8t+\lambda)>0.$$

After simplifying, we have

 $4\theta^2\beta^2 t\gamma + 3\theta^3\beta^3\gamma^2 > 0,$ 

which proves part (ii) of Proposition 1. This completes the proof of Proposition 1.

#### B.2. Proof of Proposition 2

**Part (i).** This part of the Proposition 2 claims that the consumer demand for the pay (free) media platform is lower (higher) in regime A than in regime B, i.e.,  $n_p^{A*} < n_p^{B*}$  and  $n_f^{A*} > n_f^{B*}$ . First, we prove the claim for the pay media platform. Hence,

$$n_p^{A*} < n_p^{B*} \Longleftrightarrow rac{ heta t(4t+3\lambda)}{(2t+\lambda)(8t+\lambda)} < rac{ heta (4t+3\lambda)}{8(2t+\lambda)}.$$

We rearrange the inequality in the following way and obtain

$$\theta t(4t+3\lambda)8(2t+\lambda)-(2t+\lambda)(8t+\lambda)\theta(4t+3\lambda)<0.$$

After simplifying we get

$$-\lambda\theta(4t+3\lambda)(2t+\lambda)<0$$

and conclude  $n_p^{A*} < n_p^{B*}$ . By noting that  $n_f^{k*} = \theta - n_f^{k*}, k \in \{A, B\}$ , it immediately follows that the consumer demand for the free media platform is higher in regime A than in regime B, i.e.,  $n_f^{A*} > n_f^{B*}$ .

**Part (ii).** This part of Proposition 2 claims that the advertising level in regime A exceeds that in regime B, i.e.,  $a_f^{A*} > a_f^{B*}$ . Hence,

$$a_f^{A*} > a_f^{B*} \Longleftrightarrow \frac{2\theta t\beta(3t+\lambda)}{(2t+\lambda)(8t+\lambda)} > \frac{\theta t\beta(12t+5\lambda)}{4(2t+\lambda)(4t+\lambda)}$$

We rearrange the inequality in the following way and obtain

$$\begin{aligned} &2\theta t\beta(3t+\lambda)4(2t+\lambda)(4t+\lambda)\\ &-(2t+\lambda)(8t+\lambda)\theta t\beta(12t+5\lambda)>0. \end{aligned}$$

After simplifying we get

 $3t(2t+\lambda)\theta^3\beta^3\gamma^2 > 0.$ 

and it follows that part (ii) of Proposition 2 holds. This completes the proof of Proposition 2.

#### B.3. Proof of Proposition 3

**Part (i).** To prove part (i) of Proposition 3, that is, the free media platform realizes a higher profit in regime A than in regime B  $(\pi_f^{A*} > \pi_f^{B*})$ , we have to show that

$$\frac{2t\theta^2\beta^2(3t+\lambda)^2}{(2t+\lambda)(8t+\lambda)^2} > \frac{t\theta^2\beta^2(12t+5\lambda)^2}{32(2t+\lambda)(4t+\lambda)^2}.$$

We rearrange the inequality in the following way and obtain

$$\begin{split} & 2t\theta^2\beta^2(3t+\lambda)^232(2t+\lambda)(4t+\lambda)^2 \\ & -(2t+\lambda)(8t+\lambda)^2t\theta^2\beta^2(12t+5\lambda)^2 > 0 \end{split}$$

After simplifying we get

$$t\theta^{2}\beta^{2}(2t+\lambda)(768t^{3}\lambda+1008t^{2}\lambda^{2}+376t\lambda^{3}+39\lambda^{4})>0.$$

Equivalently, for the proof of the other claim in part (i), i.e., the profit of the pay media platform is higher in regime B than in regime A  $(\pi_p^{A*} < \pi_p^{B*})$ , one has to show

$$\frac{\theta t^2 (4t+3\lambda)^2}{(2t+\lambda)(8t+\lambda)^2} < \frac{\theta t (4t+3\lambda)^2}{16(2t+\lambda)(4t+\lambda)}$$

We rearrange the inequality in the following way and obtain

$$\begin{aligned} \theta t^2 (4t+3\lambda)^2 \mathbf{16} (2t+\lambda) (4t+\lambda) \\ &- (2t+\lambda) (8t+\lambda)^2 \theta t (4t+3\lambda)^2 < \mathbf{0}. \end{aligned}$$

After simplifying we get

$$-\theta\lambda^2 t (4t+3\lambda)^2 (2t+\lambda) < 0$$

and it follows that part (i) of Proposition 3 holds.

**Part (ii).** To prove part (ii) of Proposition 3  $(\Pi^{A*} > \Pi^{B*} \Leftrightarrow \gamma < \gamma^{\pi})$ , first let  $\Pi^{A*} - \Pi^{B*} \equiv H$  with  $\Pi^{A*} = \pi_p^{A*} + \pi_f^{A*}$  and  $\Pi^{B*} = \pi_p^{B*} + \pi_f^{B*}$ . One can calculate that  $H = \frac{\kappa_1}{\kappa_2}I$ , where

 $\kappa_1 = \theta^3 \beta^2 \gamma t (4t + 3\lambda) \quad \text{and} \ \kappa_2 = 32(2t + \lambda)(4t + \lambda)^2 (8t + \lambda)^2,$  $I = 32t^2 (6\beta - \gamma) + 4t(27\beta - 8\gamma)\lambda + (13\beta - 6\gamma)\lambda^2.$ 

We now derive the following properties:

(1)  $\frac{\kappa_1}{\kappa_2} > \mathbf{0} \forall \gamma \in (\mathbf{0}, \infty).$ (2)  $\lim_{\gamma\to\infty} H = \lim_{\gamma\to\infty} I = -\infty.$ (3)  $I(\gamma = 0) = 192t^2\beta > 0$ . (4)  $I(\gamma)$ points has two critical with  $\gamma_1 = \frac{-32\theta t\beta + 13\theta^2 \beta^3 - \sqrt{448\theta^2 t^2 \beta^2 + 1112t\theta^3 \beta^4 + 169\theta^4 \beta^6}}{18\theta^2 q^2}$ and  $\gamma_2 =$  $18\theta^2 \beta^2$  $\frac{-32 \theta t \beta + 13 \theta^2 \beta^3 + \sqrt{448 \theta^2 t^2 \beta^2 + 1112 \theta^3 t \beta^4 + 169 \theta^4 \beta^6}}{18 \theta^2 \beta^2}.$  Moreover,  $\gamma_1$  is a global minimum and  $\gamma_2$  is a global maximum because  $\frac{\partial^2 I}{\partial \gamma^2}\Big|_{\gamma=\gamma_1} = 2\sqrt{\theta^2 \beta^2 (448t^2 + 1112\theta t \beta^2 + 169\theta^2 \beta^4)} > 0$ and  $\frac{\partial^2 I}{\partial \gamma^2}\Big|_{\gamma=\gamma_2} = -2\sqrt{\theta^2 \beta^2 (448t^2 + 1112\theta t \beta^2 + 169\theta^2 \beta^4)}$  $\begin{array}{c} <\mathbf{0},\\ (5) \left.\frac{\partial l}{\partial \gamma}\right|_{\gamma=0} = 4t(27\theta\beta^2 - 8t), \end{array}$ 

we thus distinguish three different cases:

(5.1) If 
$$\frac{\partial l}{\partial \gamma}\Big|_{\gamma=0} < 0$$
, then  $\gamma_1 < 0$  and  $\gamma_2 < 0$  with  $\gamma_1 < \gamma_2$ .  
(5.2) If  $\frac{\partial l}{\partial \gamma}\Big|_{\gamma=0} > 0$ , then  $\gamma_1 < 0$  and  $\gamma_2 > 0$  with  $\gamma_1 < \gamma_2$ .  
(5.3) If  $\frac{\partial l}{\partial \gamma}\Big|_{\gamma=0} = 0$ , then  $\gamma_1 < 0$  and  $\gamma_2 = 0$  with  $\gamma_1 < \gamma_2$ .

From (1) to (5) it follows that  $\Pi^{A*} < \Pi^{B*}$  if and only if  $\gamma$  exceeds a critical level  $\gamma_{crit}$ . For all values of  $\gamma$  smaller than  $\gamma_{crit}$  it is the case that  $\Pi^{A*} > \Pi^{B*}$ . This completes the proof of Proposition 3.

#### B.4. Proof of Proposition 4

**Part (i).** This part of Proposition 4 states that media consumers enjoy higher surpluses in regime B than in regime A ( $CS^{A_*} < CS^{B_*}$ ). To prove it, we need to derive

$$\left(\nu-\frac{5t}{2}+\mu_1\right)\theta < \left(\nu-\frac{103t}{64}+\mu_2\right)\theta.$$

We rearrange the inequality in the following way and obtain

$$-\frac{5t}{2}+\mu_1+\frac{103t}{64}-\mu_2<0,$$

with

$$\mu_{1} = \frac{19t^{3} + 8\lambda t^{2}}{27(2t+\lambda)^{2}} + \frac{10(326t^{3} + 37\lambda t^{2})}{27(8t+\lambda)^{2}} \text{ and}$$
$$\mu_{2} = \frac{11t^{3} + 5\lambda t^{2}}{16(2t+\lambda)^{2}} + \frac{4t^{2}}{4t+\lambda}.$$

After simplifying, we get

$$-\frac{t\lambda(4t+3\lambda)(256t^{3}+528\lambda t^{2}+224t\lambda^{2}+19\lambda^{3})}{64(2t+\lambda)^{2}(4t+\lambda)(8t+\lambda)^{2}}<0$$

#### It follows that part (i) of Proposition 4 is true.

**Part (ii).** This part of Proposition 4 indicates a higher advertisers surplus in regime A than in regime B, i.e.,  $AS^{A*} > AS^{B*}$ . Hence, we have to show that

$$\frac{2\theta^{2}t^{2}\beta^{2}(3t+\lambda)^{2}}{(2t+\lambda)^{2}(8t+\lambda)^{2}} > \frac{\theta^{2}t^{2}\beta^{2}(12t+5\lambda)^{2}}{32(2t+\lambda)^{2}(4t+\lambda)^{2}}$$

We rearrange the inequality in the following way and obtain

$$\begin{aligned} &2\theta^2 t^2 \beta^2 (3t+\lambda)^2 32 (2t+\lambda)^2 (4t+\lambda)^2 \\ &- (2t+\lambda)^2 (8t+\lambda)^2 \theta^2 t^2 \beta^2 (12t+5\lambda)^2 \\ &> 0. \end{aligned}$$

After simplifying, we get

 $\theta^3\beta^3t^2\gamma(2t+\lambda)^2(4t+3\lambda)(192t^2+108t\lambda+13\lambda^2)>0.$ 

It follows that part (ii) of Proposition 4 is true. This completes the proof of Proposition 4.

#### B.5. Proof of Proposition 5

We derive social welfare in regimes A and B as

$$W^{A*} = \frac{\theta}{54} (54\nu - 135t + \Psi_1 + \Psi_2) \text{ and}$$
$$W^{B*} = \frac{\theta}{64} (64\nu - 67t + \Psi_3 + \Psi_4)$$

with

$$\begin{split} \Psi_{1} &= \frac{3t^{2}(2t+\theta\beta^{2})}{(2t+\lambda)^{2}} + \frac{2t(11t+4\theta\beta^{2})}{(2t+\lambda)}, \\ \Psi_{2} &= \frac{20t(61t+5\theta\beta^{2})}{(8t+\lambda)} - \frac{375t^{2}(8t+\theta\beta^{2})}{(8t+\lambda)^{2}} \\ \Psi_{3} &= \frac{2t^{2}(2t+\theta\beta^{2})}{(2t+\lambda)^{2}} + \frac{2t(14t+5\theta\beta^{2})}{(2t+\lambda)}, \\ \Psi_{4} &= \frac{8t(16t+5\theta\beta^{2})}{(4t+\lambda)} - \frac{32t^{2}\theta\beta^{2}}{(4t+\lambda)^{2}}. \end{split}$$

If  $\gamma = 0$ , then  $W^{A*} = W^{B*} = \frac{\theta}{128}(128\nu + 27\theta\beta^2 - 40t)$ . Moreover, we derive

$$\frac{\partial W^{A*}}{\partial \gamma} = \frac{\theta^2 t \beta}{27} (\Psi_5 - \Psi_6) < 0 \text{ and } \frac{\partial W^{B*}}{\partial \gamma} = \frac{\theta^2 t \beta}{64} (\Psi_7 - \Psi_8) < 0$$

with

$$\begin{split} \Psi_{5} &= \frac{375t(8t+\theta\beta^{2})}{(8t+\lambda)^{3}} - \frac{10(61t+5\theta\beta^{2})}{(8t+\lambda)^{2}}, \\ \Psi_{6} &= \frac{3t(2t+\theta\beta^{2})}{(2t+\lambda)^{3}} + \frac{11t+4\theta\beta^{2}}{(2t+\lambda)^{2}}, \\ \Psi_{7} &= \frac{64t\theta\beta^{2}}{(4t+\lambda)^{3}} - \frac{8(16t+5\theta\beta^{2})}{(4t+\lambda)^{2}}, \\ \Psi_{8} &= \frac{4t(2t+\theta\beta^{2})}{(2t+\lambda)^{3}} + \frac{28t+10\theta\beta^{2}}{(2t+\lambda)^{2}}. \end{split}$$

In addition,

$$\begin{split} &\frac{\partial^2 W^{A*}}{\partial \gamma^2} = \frac{\theta^3 t \beta^2}{27} \left( \Psi_9 + \Psi_{10} \right) > 0 \quad \text{and} \\ &\frac{\partial^2 W^{B*}}{\partial \gamma^2} = \frac{\theta^3 t \beta^2}{32} \left( \Psi_{11} + \Psi_{12} \right) > 0, \end{split}$$

with

$$\begin{split} \Psi_{9} &= \frac{20(61t+5\theta\beta^{2})}{(8t+\lambda)^{3}} - \frac{1125t(8t+\theta\beta^{2})}{(8t+\lambda)^{4}} \\ \Psi_{10} &= \frac{9t(2t+\theta\beta^{2})}{(2t+\lambda)^{4}} + \frac{22t+8\theta\beta^{2}}{(2t+\lambda)^{3}}, \\ \Psi_{11} &= \frac{6t(2t+\theta\beta^{2})}{(2t+\lambda)^{4}} + \frac{28t+10\theta\beta^{2}}{(2t+\lambda)^{3}}, \\ \Psi_{12} &= \frac{8(16t+5\theta\beta^{2})}{(4t+\lambda)^{3}} - \frac{96t\theta\beta^{2}}{(4t+\lambda)^{4}}. \end{split}$$

Hence, welfare is a strictly concave function in  $\gamma$ . Moreover,

$$\frac{\partial W^{A_*}}{\partial \gamma}\Big|_{\gamma=0} = -\frac{\theta^2 \beta (136t + 27\theta \beta^2)}{512t} < 0 \text{ and}$$
$$\frac{\partial W^{B_*}}{\partial \gamma}\Big|_{\gamma=0} = -\frac{\theta^2 (32t\beta + 9\theta \beta^3)}{128t} < 0.$$

For  $\theta > \theta' = \frac{8t}{9\beta^2}$ , we derive  $\frac{\partial W^{A*}}{\partial \gamma}\Big|_{\gamma=0} > \frac{\partial W^{B*}}{\partial \gamma}\Big|_{\gamma=0}$ . Hence, at  $\gamma = 0$ , welfare in regime A decreases less strongly in  $\gamma$  than welfare in regime B. It follows that  $W^{A*} > W^{B*}$  for low values of  $\gamma$ . Increasing the parameter  $\gamma$ , numerical simulations show that there exists a critical value  $\gamma^*$  such that  $\frac{\partial W^{B*}}{\partial \gamma} > \frac{\partial W^{A*}}{\partial \gamma} \forall \gamma > \gamma^*$ . It follows that there must exist another critical value  $\gamma^W$  such that  $W^{B*} > W^{A*} \forall \gamma > \gamma^W$ . For  $\theta \leq \theta' = \frac{8t}{9\beta^2}$ , we derive  $\frac{\partial W^{A*}}{\partial \gamma}\Big|_{\gamma=0} < \frac{\partial W^{B*}}{\partial \gamma}\Big|_{\gamma=0}$ . Hence, at  $\gamma = 0$ , welfare in regime B decreases less strongly in  $\gamma$  than welfare in regime A. Furthermore, numerical simulations show that this is true for all  $\gamma > 0$ . It follows that  $W^{B*} > W^{A*} \forall \gamma > 0$ . This completes the proof of Proposition 5.

#### Appendix C. Symmetric competition

Suppose there are two symmetric free media platforms, denoted by i and j. We use the same notation from our model of asymmetric competition and derive the consumer demand for each platform as

$$n_{f,i} = \frac{\theta}{2} \left[ 1 + \frac{1}{t} (\gamma a_{f,j} - \gamma a_{f,i}) \right] \text{ and}$$
$$n_{f,j} = \frac{\theta}{2} \left[ 1 + \frac{1}{t} (\gamma a_{f,i} - \gamma a_{f,j}) \right].$$

Consumer surplus is

$$CS = \theta \left( \int_0^{\bar{x}} (\nu - \gamma a_{f,i} - tz) dz + \int_{\bar{x}}^1 (\nu - \gamma a_{f,j} - t(1-z)) dz \right).$$

We adopt the prevailing assumption of multi-homing of advertisers (e.g., Armstrong, 2006; Peitz and Valletti, 2008), which implies that the advertiser demand is independent of which platform attracts more consumers and is given by  $a_{f,i} = \beta n_{f,i} - p_{f,i}$  and  $a_{f,j} = \beta n_{f,j} - p_{f,j}$ . Overall advertiser surplus is then computed as

$$AS = \int_0^{a_{f,i}} (\beta n_{f,i} - y - p_{f,i}) dy + \int_0^{a_{f,i}} (\beta n_{f,i} - y - p_{f,i}) dy.$$

Both media platforms choose their advertising prices in both regimes so as to maximize profits. With a similar equilibrium analysis as under asymmetric competition, we obtain the relevant outcomes in the two regimes as follows: <sup>15</sup>

Regime A:

$$\begin{split} R_{f,i}^{A*} &= R_{f,j}^{A*} = \frac{\theta\beta(t+\lambda)}{4t+3\lambda}, \quad a_{f,i}^{A*} = a_{f,j}^{A*} = \frac{\theta\beta(2t+\lambda)}{8t+6\lambda}, \\ \Pi^{A*} &= \frac{\theta^2\beta^2(2t+\lambda)(t+\lambda)}{(4t+3\lambda)^2}, \\ CS^{A*} &= \theta\left(\nu + \frac{16t^2}{36(4t+3\lambda)} - \frac{\lambda}{6} - \frac{13t}{36}\right), \\ AS^{A*} &= \frac{\theta^2\beta^2(2t+\lambda)^2}{4(4t+3\lambda)^2}, \quad \text{and} \\ W^{A*} &= \theta\left(\nu + \frac{\theta\beta(5\beta-6\gamma)}{36} + \frac{t}{36}\left(\frac{16t}{4t+3\lambda} + \frac{4\theta\beta^2(7t+6\lambda)}{(4t+3\lambda)^2} - 13\right)\right). \end{split}$$

**Regime B:** 

$$\begin{split} r_{f,i}^{B*} &= r_{f,j}^{B*} = \frac{t + \lambda - \sqrt{t(t+\lambda)}}{\theta\gamma}, a_{f,i}^{B*} = a_{f,j}^{B*} = \frac{\sqrt{t(t+\lambda)} - t}{2\gamma}, \\ \Pi^{B*} &= \frac{\left(t + \lambda - \sqrt{t(t+\lambda)}\right)\left(\sqrt{t(t+\lambda)} - t\right)}{4\gamma^2}, \\ \mathrm{CS}^{B*} &= \theta\left(\nu + \frac{t}{4} - \frac{2\sqrt{t(t+\lambda)}}{4}\right), \\ \mathrm{AS}^{B*} &= \frac{t(2t + \lambda - 2\sqrt{t(t+\lambda)})}{4\gamma^2}, \quad \mathrm{and} \\ W^{B*} &= \frac{1}{4\gamma^2}\left(t\left(\theta\beta(\gamma - 3\beta) + 2\sqrt{t(t+\lambda)}\right)\right) \\ &+ 2\theta\gamma\left(2\nu\gamma + (\beta - \gamma)\sqrt{t(t+\lambda)}\right) - 2t^2\right). \end{split}$$

<sup>&</sup>lt;sup>15</sup> Note that in both regimes the platforms share the equilibrium consumer demand equally, i.e.,  $n_{B^*}^{A^*} = n_{B^*}^{A^*} = n_{B^*}^{B^*} = n_{B^*}^{A^*} = \frac{N}{2}$ .

A comparison of the equilibrium outcomes in both regimes leads to the conclusions drawn in Section 6.1.

#### References

- Anderson, S., Coate, S., 2005. Market provision of broadcasting: a welfare analysis. Review of Economic Studies 72, 947–972.
- Anderson, S., Gabszewicz, J., 2006. The media and advertising: a tale of two-sided markets. Handbook on the Economics of Art and Culture 1, 567–614.
- Armstrong, M., 2006. Competition in two-sided markets. RAND Journal of Economics 37 (3), 668–691.
- Belleflamme, P., Toulemonde, E., 2009. Negative intra-side externalities in two-sided markets. International Economic Review 50 (1), 245–272.
- Caillaud, B., Jullien, B., 2003. Chicken & egg: competition among intermediation service providers. RAND Journal of Economics 34 (2), 309–328.
- Casadesus-Masanell, R., Zhu, F., 2010. Strategies to fight ad-sponsored rivals. Management Science 56 (9), 1484–1499.
- Choi, J., 2006. Broadcast competition and advertising with free entry: subscription vs. free-to-air. Information Economics and Policy 18 (2), 181–196.
- Crampes, C., Haritchabalet, C., Jullien, B., 2009. Advertising, competition and entry in media industries. Journal of Industrial Economics 57 (1), 7–31.
- Depken II, C., Wilson, D., 2004. Is advertising a good or a bad? Evidence from US magazine subscriptions. Journal of Business 77 (2), 61–80.
- Dietl, H., Lang, M., Lin, P., 2012. The Effects of Introducing Advertising in Pay TV: A Model of Asymmetric Competition between Pay TV and Free TV. ISU Working Paper No. 153, University of Zurich.
- Economides, N., Tåg, J., 2012. Network neutrality on the internet: a twosided market analysis. Information Economics and Policy 24, 91–104.
- Gabszewicz, J., Laussel, D., Sonnac, N., 2001. Press advertising and the ascent of the "Pensee Unique". European Economic Review 45 (4–6), 641–651.
- Gabszewicz, J., Laussel, D., Sonnac, N., 2004. Programming and advertising competition in the broadcasting industry. Journal of Economics & Management Strategy 13 (4), 657–669.

- Hagiu, A., 2006. Pricing and commitment by two-sided platforms. Rand Journal of Economics 37 (3), 720–737.
- Kaiser, U., Song, M., 2009. Do media consumers really dislike advertising? An empirical assessment of the role of advertising in print media markets. International Journal of Industrial Organization 27 (2), 292– 301.
- Kaiser, U., Wright, J., 2006. Price structure in two-sided markets: evidence from the magazine industry. International Journal of Industrial Organization 24 (1), 1–28.
- Kind, H., Nilssen, T., Sorgard, L., 2007. Competition for viewers and advertisers in a TV oligopoly. Journal of Media Economics 20 (3), 211– 233.
- Kind, H., Nilssen, T., Sorgard, L., 2009. Business models for media firms: does competition matter for how they raise revenue? Marketing Science 28 (6), 1112–1128.
- Li, T., 2009. Tying in Two-Sided Markets. Toulouse School of Economics Working Paper Series.
- Lin, P., 2011. Market provision of program quality in the television broadcasting industry. The BE Journal of Economic Analysis & Policy (Contributions) 11 (1), 1–17.
- Peitz, M., Valletti, T., 2008. Content and advertising in the media: pay-tv versus free-to-air. International Journal of Industrial Organization 26 (4), 949–965.
- Reisinger, M., 2011. Platform competition for advertisers and users in media markets. International Journal of Industrial Organization 30 (2), 243–252.
- Rochet, J., Tirole, J., 2003. Platform competition in two-sided markets. Journal of the European Economic Association 1 (4), 990–1029.
- Rysman, M., 2004. Competition between networks: a study of the market for yellow pages. Review of Economic Studies 71 (2), 483–512.
- Tåg, J., 2009a. Competing platforms and third party application developers. Communications & Strategies 1 (74), 95–114.
- Tåg, J., 2009b. Paying to remove advertisements. Information Economics and Policy 21 (4), 245–252.
- Weyl, E.G., 2010. A price theory of multi-sided platforms. American Economic Review 100 (4), 1642–1672.
- Wilbur, K., 2008. A two-sided, empirical model of television advertising and viewing markets. Marketing Science 27 (3), 356–378.